

provided all the resistance values and other temperatures are known.<sup>3</sup> Consider the network of Fig. 1. By straightforward network analysis one obtains for  $v_0$  and  $v_2$ :

$$(2a) \quad v_0 = \frac{Z_0}{Z_T} [i_0(Z_1 + Z_2) - i_1 Z_1 - i_2 Z_2]$$

$$(2b) \quad v_2 = \frac{Z_2}{Z_T} [i_0 Z_0 + i_1 Z_1 - i_2(Z_1 + Z_0)]$$

where

$$Z_T = Z_0 + Z_1 + Z_2, \quad Z_0 = R_0 / (1 + j\omega C_0 R_0), \text{ etc.}$$

and  $v_0$ ,  $i_0$ , etc. are complex vectors. If one multiplies  $v_0$  and  $v_2$  and takes the time average over the product, then one forms:

$$(3) \quad \text{Re}(\overline{v_0 v_2^*}) = \text{Re} \left\{ \frac{Z_0 Z_2^*}{|Z_T|^2} [ |i_0|^2 Z_0^* (Z_1 + Z_2) + |i_2|^2 Z_2 (Z_0^* + Z_1^*) - |i_1|^2 |Z_1|^2 ] \right\},$$

where

$$|i_0|^2 = 4kT_0 df / R_0$$

(the Planck factor is assumed to be unity), similarly  $|i_1|^2$  and  $|i_2|^2$ . The time average of the products  $\text{Re}(i_0 i_1^*)$ , etc. are zero because the resistors are independent noise sources. The product  $\text{Re}(\overline{v_0 v_2^*})$  appearing in equation (3) corresponds to the direct multiplication of the physical voltages  $v_0$  and  $v_2$ . From equation (3) one sees that if either  $R_0 C_0 = R_1 C_1 = R_2 C_2$  or  $(\omega R_n C_n)^2 \ll 1$  the product  $\text{Re}(\overline{v_0 v_2^*})$  can have a positive or a negative sign provided  $T_1 > (T_0 + T_2)$ . For either of the above conditions the value of  $R_1$  required to make  $\text{Re}(\overline{v_0 v_2^*}) = 0$  can be calculated from equation (3):

$$(4) \quad R_1 = \frac{T_0 R_2 + T_2 R_0}{T_1 - T_0 - T_2}$$

In this experiment  $R_0$  and  $R_2$  were both kept in the helium bath so that  $T_0 = T_2$ .  $R_2$  and  $R_0$  were matched to better than 1/2%, and  $T_1$  was in an isothermal bath at room temperature. If  $T_1$  and the resistances are measured,  $T_0$  can be calculated from

$$(5) \quad T_0 = T_1 \frac{R_1}{R_0 + 2R_1 + R_2}$$

## II. THE THERMOMETER AND EXPERIMENTAL PROCEDURES

The first requirement for an absolute noise thermometer of the kind described above is to find some resistors which are stable at liquid helium temperatures, whose values are preferably reproducible for several experiments, which produce no noise in addition to thermal noise, and whose resistive component

<sup>3</sup>This idea was proposed by Dr. J. B. Garrison to Prof. A. W. Lawson of Chicago University (verbal communication by Prof. R. E. Burgess).